

MAXIMUM POWER TRACKING TECHNIQUE FOR SOLAR PANELS

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FIELD OF THE INVENTION

This invention relates to method and apparatus for efficiently extracting the maximum output power from a solar panel under varying meteorological and load conditions.

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BACKGROUND OF THE INVENTION

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The solar panel is the fundamental energy conversion component of photovoltaic (PV) systems which have been used in many applications, such as the aerospace industry, electric vehicles, communication equipment, and others. As solar panels are relatively expensive, it is important to improve the utilization of solar energy by solar panels and to increase the efficiency of PV systems. Physically, the power supplied by the panels depends on many extrinsic factors, such as insolation (incident solar radiation) levels, temperature, and load condition. Thus, a solar panel is typically rated at an insolation level together with a specified temperature, such as 1000W/m^2 at 25°C . The electrical power output of a solar panel usually increases linearly with the insolation and decreases with the cell / ambient temperature.

PRIOR ART

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In practice, there are three possible approaches for maximizing the solar power extraction in medium- and large-scale PV systems. They are sun tracking, maximum power point (MPP) tracking or both. For the small-scale systems, the use of MPP

tracking only is popular for the economical reason. In the last two decades, various methods including power-matching schemes, curve-fitting techniques, perturb-and-observe methods, and incremental conductance algorithms have been proposed for tracking the MPP of solar panels.

Power-matching schemes require the selected solar panels to have suitable output characteristics or configurations that can be matched with particular loads. However, these techniques only approximate the location of the MPP because they are basically associated with specific insolation and load conditions. Curve-fitting techniques require prior examination of the solar panel characteristics, so that an explicit mathematical function describing the output characteristics can be predetermined. Proposed prior methods are based on fitting the operating characteristic of the panel to the loci of the MPP of the PV systems. Although these techniques attempt to track the MPP without computing the voltage-current product explicitly for the panel power, curve-fitting techniques cannot predict the characteristics including other complex factors, such as aging, temperature, and a possible breakdown of individual cells.

The perturb-and-observe (PAO) method is an iterative approach that perturbs the operation point of the PV system, in order to find the direction of change for maximizing the power. This is achieved by periodically perturbing the panel terminal voltage and comparing the PV output power with that of the previous perturbation cycle. Maximum power control is achieved by forcing the derivative of the power to be equal to zero under power feedback control. This has an advantage of not requiring the solar panel characteristics. However, this approach is unsuitable for applications in rapidly changing atmospheric conditions. The solar panel power is measured by multiplying its voltage

and current, either with a microprocessor or with an analog multiplier. In certain prior methods, the tracking technique is based on the fact that the terminal voltage of the solar panels at MPP is approximately at 76% of the open-circuit voltage, but this means that in order to locate the MPP, the panel is disconnected from the load momentarily so that the open-circuit voltage can be sampled and kept as reference for the control loop.

The disadvantages of the PAO method can be mitigated by comparing the instantaneous panel conductance with the incremental panel conductance. This method is the most accurate one among the above prior art methods and is usually named as the incremental conductance technique (ICT). The input impedance of a switching converter is adjusted to a value that can match the optimum impedance of the connected PV panel. This technique gives a good performance under rapidly changing conditions. However, the implementation is usually associated with a microcomputer or digital signal processor that usually increases the whole system cost.

SUMMARY OF THE INVENTION

According to the present invention there is provided a method for tracking the maximum power point of a solar panel, comprising:

- (a) providing a pulsewidth-modulated (PWM) DC/DC converter between the output of said panel and a load, and
- (b) introducing a perturbation into a switching parameter of said converter.

In a first embodiment of the invention the parameter is the duty cycle of at least one switching device in the converter. In a second embodiment of the invention the parameter is the switching frequency of at least one switching device in the converter.

According to another aspect of the invention there is provided apparatus for tracking the maximum power point of a solar panel, comprising:

- (a) a pulsewidth-modulated (PWM) DC/DC converter between the output of the solar panel and a load, and
- 5 (b) means for introducing a perturbation into a switching parameter of said converter.

In the first embodiment of the invention the converter operates in switching mode and said perturbation means comprises means for introducing a perturbation into the duty cycle of at least one switching device in the said converter. In a second embodiment of the invention the converter operates in switching mode and said perturbation means comprises means for introducing a perturbation into the switching frequency of at least one switching device in the said converter.

BRIEF DESCRIPTION OF THE DRAWINGS

15 Some examples of the present invention will now be described by way of example and with reference to the accompanying drawings, in which:

Fig.1 is an equivalent circuit of a solar-panel connected to a converter,

Fig.2 is a circuit diagram of a SEPIC converter,

Fig.3 illustrates the operating principles of a SEPIC converter,

20 Fig.4 is a block diagram of a first embodiment of the invention,

Fig.5 illustrates an experimental set-up,

Figs.6(a) & (b) illustrate solar panel characteristics in the first embodiment,

Figs.7(a) & (b) show converter waveforms in the first embodiment,

Figs.8(a) & (b) show further converter waveforms in the first embodiment,

Figs.9(a) & (b) show further converter waveforms in the first embodiment,

Fig.10 shows further converter waveforms in the first embodiment,

Fig.11 is a comparison of maximum solar panel output power using the first
embodiment with ideal power output,

Fig.12 is a circuit diagram of a Cuk converter,

Fig.13 illustrates the relationship between ϵ_1/β and k ,

Fig.14 is a block diagram of a method and apparatus for MPP tracking according
to a second embodiment of the invention,

Fig.15 illustrates the relationship between ϵ_2/β and k' ,

Fig.16 illustrates an experimental set up,

Fig.17 shows the performance of a solar panel with MPP tracking according to the
second embodiment of the invention,

Figs.18(a) and (b) show converter waveforms in the second embodiment of the
invention with the converter in DICM and DCVM modes respectively,

Figs.19(a)-(d) show converter waveforms in the second embodiment of the
invention with the converter in DICM ((a) and (c)) and DCVM ((b) and (d))
modes respectively,

Figs.20(a) and (b) show further converter waveforms in the second embodiment
with the converter in DICM and DCVM modes respectively, and

Figs.21(a) and (b) show further converter waveforms in the second embodiment
with the converter in DICM and DCVM modes respectively.

DETAILED DESCRIPTION OF PREFERRED EMBODIMENTS

Before describing a first embodiment of the invention in detail, a theoretical explanation of the principles underlying the present invention is provided.

5 A. Derivation of the required dynamic input characteristics of a converter at MPP

Fig. 1 shows an equivalent circuit of the solar panel connected to a converter. The solar panel is represented by a voltage source v_g connected in series with an output resistance r_g at the MPP. The input voltage and the equivalent input resistance of the converter are v_i and r_i , respectively. As the input power P_i to the converter is equal to the
10 output power P_o of the solar panel,

$$P_i = P_o = \frac{v_i^2}{r_i} \quad (1)$$

The rate of change of P_i with respect to v_i and r_i can be shown to be

$$\partial P_i = 2 \frac{v_i}{r_i} \partial v_i - \frac{v_i^2}{r_i^2} \partial r_i \quad (2)$$

At the MPP, the rate of change of P_i equals zero. Hence,

$$15 \quad \partial P_i = 0 \quad \Rightarrow \quad \frac{\partial v_i}{\partial r_i} = \frac{V_i}{2 R_i} \quad (3)$$

where V_i and R_i are the input voltage and the input resistance at MPP.

The above equation gives the required dynamic input characteristics of the converter at the MPP. The input voltage will have a small-signal variation of δv_i if the input resistance is subject to a small-signal change of δr_i . That is,

$$20 \quad \frac{\delta v_i}{\delta r_i} \approx \frac{\partial v_i}{\partial r_i} = \frac{V_i}{2 R_i} \quad (4)$$

In the following sections, a SEPIC converter is illustrated. It will be understood, however, that similar techniques can be applied to other converters, such as Cuk, buck-boost, buck, and boost converters.

5 B. Input resistance and voltage stress of a SEPIC converter

Fig. 2 shows the circuit diagram of a SEPIC converter. If the converter is operated in discontinuous capacitor voltage (DCV) mode, there are in total three circuit topologies in one switching cycle (d). The sequence of operation and the waveforms are shown in Fig. 3. If the two inductor currents (i.e., I_1 and I_2) are assumed to be constant, the capacitor voltage $v_C(t)$ and diode voltage $v_D(t)$ in the respective three operating intervals can be expressed as

$$v_C(t) = \begin{cases} \frac{I_1(1-d)T_S}{C} - V_o - \frac{I_2}{C}t & 0 < t < d_1 T_S \\ -V_o & d_1 T_S < t < d T_S \\ \frac{I_1}{C}(t - d T_S) - V_o & d T_S < t < T_S \end{cases} \quad (5a)$$

$$v_D(t) = \begin{cases} V_o + v_C(t) & 0 < t < d_1 T_S \\ 0 & d_1 T_S < t < T_S \end{cases} \quad (5b)$$

As $v_C(d_1 T_S) = -V_o$,

$$\begin{aligned} \frac{I_1(1-d)T_S}{C} - V_o - \frac{I_2}{C}d_1 T_S &= -V_o \\ \Rightarrow d_1 &= \frac{I_1}{I_2}(1-d) \end{aligned} \quad (6)$$

Under the steady-state condition, the average voltage across L_2 is zero. Hence, the V_o is equal to the average value of v_D . That is,

$$V_o = \frac{1}{T_S} \int_0^{d_1 T_S} v_D(t) dt = \frac{T_S}{2C} I_1 (1-d) d_1 \quad (7)$$

As the average voltage across L_1 is also zero,

$$v_i = \frac{1}{T_S} \int_0^{T_S} v_C(t) dt = \frac{T_S}{2C} I_1 (1-d)^2 \quad (8)$$

Hence, the input resistance r_i of the converter is

$$r_i = \frac{v_i}{I_1} = \frac{(1-d)^2}{2C f_S} \quad (9)$$

where $f_S = 1 / T_S$ is the switching frequency.

5 Moreover, the voltage stress across the main switch S , v_{stress} , equals

$$v_{stress} = v_C(T_S) + V_o = \frac{I_1}{C} (1-d) T_S = \frac{2}{1-d} v_i \quad (10)$$

In the first embodiment of the present invention, to be described further below, equations (9) and (10) will be used to locate the MPP of a solar panel. Since, as is known, the input resistance and the voltage stress across the main switch of a Cuk converter is same as (9) and (10), respectively, both SEPIC and Cuk converters exhibit similar r_i and v_{stress} and thus they can be used to locate the MPP.

C. *Dynamic input resistance of the converter under perturbation*

If a small-signal sinusoidal perturbation δd is injected into d ,

$$15 \quad d = D + \delta d = D + \hat{d} \sin \omega t, \quad (11)$$

where $\omega = 2\pi f$ and D is the nominal duty cycle at the MPP, and \hat{d} and f are the amplitude and frequency of the injected perturbation, respectively. In the following derivations, the value of f is assumed to be much smaller than f_S .

By substituting (11) into (9), the input resistance can be expressed as

$$20 \quad r_i = \frac{(1-D)^2}{2 f_S C} - \frac{(1-D)}{f_S C} \hat{d} \sin \omega t + \frac{1}{2 f_S C} \hat{d}^2 \sin^2 \omega t \quad (12)$$

Hence, r_i includes two main components, namely the static resistance R_i at the MPP and the dynamic resistance δr_i around the MPP. Each one can be expressed as

$$R_i = \frac{(1-D)^2}{2 f_s C} \quad (13)$$

and
$$\delta r_i = -\frac{(1-D)}{f_s C} \hat{d} \sin \omega t + \frac{1}{2 f_s C} \hat{d}^2 \sin^2 \omega t \quad (14)$$

5 By substituting (14) into (4), the input voltage variation δv_i at the MPP can be expressed as

$$\delta v_i = \delta \bar{v}_i + \delta \tilde{v}_i \text{ and } \delta \tilde{v}_i = \delta \tilde{v}_{i,1} + \delta \tilde{v}_{i,2} \quad (15)$$

where $\delta \bar{v}_i = \frac{V_i}{4(1-D)^2} \hat{d}^2$, $\delta \tilde{v}_{i,1} = -\frac{V_i}{(1-D)} \hat{d} \sin \omega t$, and $\delta \tilde{v}_{i,2} = -\frac{V_i}{4(1-D)^2} \hat{d}^2 \cos 2\omega t$.

δv_i is maximum when

$$10 \quad \omega t = \frac{(2n+1)}{2} \pi, n = 1, 3, 5, \dots \quad (16)$$

Its maximum value $\delta \tilde{v}_{i,\max}$ can be shown to be equal to

$$\delta v_{i,\max} = \frac{V_i}{(1-D)} \hat{d} + \frac{V_i}{2(1-D)^2} \hat{d}^2 \quad (17)$$

Consider the ac-component of δv_i , its maximum value $\delta \tilde{v}_{i,\max}$ can be expressed as

$$\delta \tilde{v}_{i,\max} = \delta \tilde{v}_{i,m1} + \delta \tilde{v}_{i,m2} \quad (18)$$

$$15 \quad \text{where } \delta \tilde{v}_{i,m1} = \frac{V_i}{(1-D)} \hat{d} \text{ and } \delta \tilde{v}_{i,m2} = \frac{V_i}{4(1-D)^2} \hat{d}^2.$$

The ratio between the magnitude of $\delta \tilde{v}_{i,1}$ and $\delta \tilde{v}_{i,2}$, \mathfrak{R} , is

$$\mathfrak{R} = \left| \frac{\delta \tilde{v}_{i,m2}}{\delta \tilde{v}_{i,m1}} \right| = \frac{\hat{d}}{4(1-D)} \quad (19)$$

\Re is an index showing the spectral quality of the input voltage variation at the frequency of the injected perturbation with respect to the amplitude of the perturbation. The smaller the value of \Re is, the more dominant is the component of the injected frequency in δv_i .

5 D. Voltage stress of the main switch under perturbation

The maximum value of v_{stress} (i.e., $v_{stress,max}$) under a sinusoidal perturbation can be obtained by substituting $d = D + \delta d$ and $v_i = V_i + \delta v_i$ into (10). Thus,

$$\begin{aligned}
 v_{stress} &= \frac{2}{(1-D-\delta d)} (V_i + \delta v_i) \\
 &= \frac{2}{(1-D)} \frac{1}{1 - \frac{\delta d}{(1-D)}} (V_i + \delta v_i) \\
 &= \frac{2}{(1-D)} \left[1 + \frac{1}{(1-D)} \delta d + \frac{1}{(1-D)^2} \delta d^2 + \dots \right] (V_i + \delta v_i) \\
 &= \frac{2}{(1-D)} V_i + \frac{2 \delta d}{(1-D)^2} \left(\frac{1}{1 - \frac{\delta d}{1-D}} \right) (V_i + \delta v_i) + \frac{2}{1-D} \delta v_i \\
 &= V_{stress} + \delta v_{stress}
 \end{aligned} \tag{20}$$

where $V_{stress} = \frac{2 V_i}{(1-D)}$ and $\delta v_{stress} = \frac{2 \delta d}{(1-D)^2} \left(\frac{1}{1 - \frac{\delta d}{1-D}} \right) (V_i + \delta v_i) + \frac{2}{1-D} \delta v_i$.

10 The maximum value of v_{stress} , $v_{stress,max}$, can be approximated by substituting $\delta d = \hat{d}$ and

$\delta v_i = \delta v_{i,max}$ in (17) into (20). It can be shown that

$$v_{stress,max} = \frac{2 V_i}{(1-D)} [1 + \varepsilon(D)] \tag{21}$$

where $\varepsilon(D) = \frac{2 \hat{d} (1-D + \frac{\hat{d}}{4})}{(1-D)(1-D-\hat{d})}$.

Comparing (18) and (21), it can be shown that

$$\delta \tilde{v}_{i,\max} = \beta v_{stress,\max}, \quad \beta = \frac{\hat{d}}{2} \left[\frac{(1-D-\hat{d})(1-D+\frac{\hat{d}}{2})}{(1-D)^2 + \hat{d}(1-D+\frac{\hat{d}}{2})} \right] \quad (22)$$

at the MPP. If $\hat{d} \ll 1 - D$, $\beta \cong \hat{d} / 2$. Thus, $\delta \tilde{v}_{i,\max}$ and $v_{stress,\max}$ form a relatively constant ratio of β at the MPP.

Fig.4 is a block diagram of apparatus for locating the MPP according to a first embodiment of the invention. First, the error amplifier compares the maximum input ripple voltage (i.e., $\delta \tilde{v}_{i,\max}$) and the attenuated switch voltage stress (i.e., $\beta' v_{stress,\max}$), and generates an error signal. Theoretically, β' should be equal to β in (22). However, as β is dependent on D , a constant value is used to represent it for the sake of simplicity in the implementation. Its value is equal to $r_2 / (r_1 + r_2)$ so that

$$\beta' = \frac{r_2}{r_1 + r_2} = \frac{1}{D_{\max} - D_{\min}} \int_{D_{\min}}^{D_{\max}} \beta(D) dD \quad (23)$$

where D_{\min} and D_{\max} are the minimum and maximum duty cycle of the main switch, respectively.

D_{\max} is determined by the minimum input resistance $R_{i,\min}$ of the converter, which is also the minimum equivalent output resistance of the solar panel. By using (9),

$$D_{\max} = 1 - \sqrt{2 R_{i,\min} C f_s} \quad (24)$$

For the converter operating in DCV mode, it must be ensured that $d_1 \leq d$. The output current I_o can be expressed as

$$I_o = \frac{V_o}{R} = (1-d) I_1 + (1-d_1) I_2 \Rightarrow I_2 = \frac{1}{1-d_1} \left[\frac{V_o}{R} - (1-d) I_1 \right] \quad (25)$$

d_1 is determined by substituting (6) and (7) into (25) and thus

$$D_{\min} = \sqrt{2 R C f_s} \quad (26)$$

Next, a small-signal sinusoidal perturbation is superimposed on the error signal and then the combined signal v_{con} is compared to a ramp function to generate a PWM gate signal to the main switch.

The tracking action can be illustrated by considering the values of $\delta \tilde{v}_{i,max}$ and

5 $v_{stress,max}$ when d does not equal D . Based on Fig. 1 and using (9), it can be shown that

$$\begin{aligned} v_i &= \frac{r_i}{r_i + r_g} v_g \\ \Rightarrow \delta v_i &= -\frac{2 r_i r_g}{(r_i + r_g)^2} \frac{v_g}{(1-d)} \delta d \end{aligned} \quad (27)$$

Thus,

$$\delta \tilde{v}_{i,max} = \frac{2 \alpha}{(1 + \alpha)^2} \frac{v_g}{(1-d)} \hat{d} \quad (28)$$

where $\alpha = r_i / r_g = [(1-d) / (1-D)]^2$.

10 By substituting (27) and (28) into (20), $v_{stress,max}$ is equal to

$$v_{stress,max} = \frac{2 \alpha [(1 + \alpha)(1-d) + 2\hat{d}]}{(1-d)(1-d-\hat{d})(1+\alpha)^2} v_g \quad (29)$$

Referring to (22), if $\hat{d} \ll 1-d$, $\beta' \cong \hat{d}/2$. It can be shown that

$$\Phi = \frac{\beta' v_{stress,max}}{\delta v_{i,max}} \cong \frac{1}{2} \left[\frac{(1+\alpha)(1-d) + 2\hat{d}}{1-d-\hat{d}} \right] \cong \frac{1}{2} (1+\alpha) = \frac{1}{2} \left[1 + \left(\frac{1-d}{1-D} \right)^2 \right] \quad (30)$$

When r_i equals r_g (i.e., $\alpha = 1$), Φ becomes unity. This is the condition when the
 15 converter is at the MPP. If d is smaller than D , r_i will be larger than r_g (i.e., $\alpha > 1$), Φ becomes larger than unity. The error amplifier will then generate a signal so as to increase the duty cycle. Conversely, if d is larger than D , r_i will be smaller than r_g (i.e., $\alpha < 1$). Φ becomes less than unity. The error amplifier will then generate a signal so as to

decrease the duty cycle. The above regulatory actions cause the feedback network to adjust the duty cycle, in order to make $\Phi = 1$ or $r_i = r_g$.

The embodiment of Fig.4 has been experimentally checked using the set-up shown in Fig.5 and using a solar panel Siemens SM-10 with a rated output power of 10W. The component values of the SEPIC converter are as shown in Fig. 4. The output resistance R equals 10Ω . The switching frequency is set at 80kHz and the injected sinusoidal perturbation frequency is 500Hz . The radiation level illuminated on the solar panel is adjusted by controlling the power of a 900W halogen lamp using a light dimmer. The bypass switch is used to give the maximum brightness from the lamp for studying the transient response. The surface temperature of the panel is maintained at about 40°C . The measured $v_g - i_g$ characteristics and the output power versus the terminal resistance of the solar panel at different power P_{lamp} to the lamp are shown in Fig. 6(a) and Fig. 6(b), respectively. Under a given P_{lamp} , it can be seen that the panel output power will be at its maximum under a specific value of the terminal resistance. When P_{lamp} equals 900W (i.e., full power), the required terminal resistance is 14Ω , in order to extract maximum power from the solar panel. Thus, by applying (24) and (26), D_{\min} and D_{\max} equal 0.274 and 0.675 , respectively. Based on (9), the variation of the input resistance is between 14Ω and 70Ω , which are well within the required tracking range of the input resistance shown in Fig. 6(b).

Detailed experimental waveforms of the gate signal, the switch voltage stress, the converter input terminal voltage, and the input inductor current in one switching cycle at the maximum lamp power are shown in Fig. 7. Macroscopic views of the switch voltage stress, input voltage, and input current are shown in Fig. 8. It can be seen that a low-

frequency variation of 500Hz is superimposed on all waveforms. They are all in close agreement with the theoretical ones. In addition, the input current is continuous. Thus, the MPP tracking method and apparatus of this embodiment of the present invention is better than the one using classical buck-type converter which takes pulsating input current. Moreover, it is unnecessary to interrupt the system, in order to test the open-circuit terminal voltage of the solar panel.

Fig. 9 shows the ac-component of the converter input terminal voltage with \Re equal to 0.02, 0.05, and 0.1, respectively. As \Re increases, the ac-component will be distorted because the second-order harmonics become dominant in (15).

In order to observe the feedback action of the proposed approach under a large-signal variation in the radiation level, P_{lamp} is changed from 500W to 900W. The transient waveform of the feedback signal is shown in Fig. 10. The settling time is about 0.4 seconds. Based on the results in Fig. 6(b), a comparison of the maximum attainable output power and the measured output power with the proposed control scheme under different P_{lamp} is shown in Fig. 11. It can be seen that the proposed control technique can track the output power of the panel with an error of less than 0.2W. A major reason for the discrepancy is due to the variation of β with respect to the duty cycle shown in (23), which will directly affect the tracking accuracy.

The methodology of this first embodiment of the invention is based on connecting a pulsewidth-modulated (PWM) DC/DC converter between a solar panel and a load or battery bus. In this embodiment a SEPIC converter operates in discontinuous capacitor voltage mode whilst its input current is continuous. By modulating a small-signal sinusoidal perturbation into the duty cycle of the main switch and comparing the

maximum variation in the input voltage and the voltage stress of the main switch, the maximum power point (MPP) of the panel can be located. The nominal duty cycle of the main switch in the converter is adjusted to a value, so that the input resistance of the converter is equal to the equivalent output resistance of the solar panel at the MPP. This approach ensures maximum power transfer under all conditions without using microprocessors for calculation.

In the first embodiment of the invention described above, a small perturbation is introduced into the duty cycle of at least one switching device in the converter. In a second embodiment of the invention, to be described in more detail below, a small perturbation may be introduced into the switching frequency of a PWM DC/DC converter. Before describing the second embodiment in more detail, further theoretical explanation is offered below. SEPIC and Cuk converters operating in discontinuous inductor current mode (DICM) and discontinuous capacitor voltage mode (DCVM) are illustrated.

A. *Discontinuous Inductor Current Mode (DICM)*

The input characteristics of SEPIC (Fig.2) and Cuk converters (Fig.12) are similar. The input resistance r_i equals

$$r_i = \frac{2L_e f_s}{d^2}, \quad (31)$$

where $L_e = L_1 // L_2$, f_s is the switching frequency, and d is the duty cycle of the switch S in Figs. 2 and 12.

By differentiating (31) with respect to f_s , it can be seen that a small change of f_s will introduce a small variation in r_i . That is,

$$\delta r_i = \frac{2L_e}{d^2} \delta f_s. \quad (32)$$

Hence, if f_s is modulated with a small-signal sinusoidal variation

$$f_s = \bar{f}_s + \delta f_s = \bar{f}_s + \hat{f}_s \sin(2\pi f_m t), \quad (33)$$

where \bar{f}_s is the nominal switching frequency, f_m is the modulating frequency and is much lower than \bar{f}_s , and \hat{f}_s is the maximum frequency deviation.

Thus, with the above switching frequency perturbation, r_i will include an average resistance R_i and a small variation δr_i . That is,

$$r_i = R_i + \delta r_i, \quad (34)$$

$$\text{where } R_i = \frac{2L_e}{d^2} \bar{f}_s, \quad (35)$$

$$\text{and } \delta r_i = \frac{2L_e}{d^2} \hat{f}_s \sin(2\pi f_m t). \quad (36)$$

Let D_{MP} be the required duty cycle of S at MPP. r_g can be expressed as

$$r_g = \frac{2L_e \bar{f}_s}{D_{MP}^2}. \quad (37)$$

By using (35) and (37),

$$V_i = \frac{R_i}{R_i + r_g} v_g = \frac{D_{MP}^2}{D_{MP}^2 + d^2} v_g \quad (38)$$

and the variation of v_i with respect to r_i becomes

$$\delta v_i \approx \frac{d}{dr_i} \left(\frac{r_i}{r_i + r_g} v_g \right) \delta r_i = \frac{r_g v_g}{(R_i + r_g)^2} \delta r_i \quad (39)$$

By substituting (32), (35), and (37) into (39), the small-signal variation on v_i is

$$\delta v_i = \frac{(D_{MP} d)^2 v_g}{(D_{MP}^2 + d^2)^2 \bar{f}_s} \delta f_s. \quad (40)$$

The peak value of δv_i (i.e., \hat{v}_i) becomes

$$\hat{v}_i = \frac{(D_{MP} d)^2 v_g}{(D_{MP}^2 + d^2)^2 \bar{f}_s} \hat{f}_s. \quad (41)$$

As v_g and r_g vary with insolation and temperature, d should be automatically

5 adjusted to D_{MP} in the controller. The following equation holds at the MPP and is obtained by substituting (32) and (35) into (30),

$$\frac{\hat{f}_s}{2 \bar{f}_s} V_i = \hat{v}_i \quad (42)$$

Based on (38) and (41), the difference, ε_1 , between the normalized characteristics

of $\frac{\hat{f}_s V_i}{2 \bar{f}_s v_g}$ and $\frac{\hat{v}_i}{v_g}$ can be shown to be equal to

$$10 \quad \varepsilon_1(k) = \frac{\hat{f}_s V_i}{2 \bar{f}_s v_g} - \frac{\hat{v}_i}{v_g} = \beta \frac{1 - k^2}{(1 + k^2)^2} \quad (43)$$

where $k = d / D_{MP}$ and $\beta = \hat{f}_s / (2 \bar{f}_s)$.

Fig. 13 shows the relationships between ε_1 / β and k . It can be concluded that,

$$\text{If } d < D_{MP} \text{ (i.e., } k < 1), \varepsilon_1(k) > 0 \quad (44a)$$

$$\text{If } d = D_{MP} \text{ (i.e., } k = 1), \varepsilon_1(1) = 0 \quad (44b)$$

$$15 \quad \text{If } d > D_{MP} \text{ (i.e., } k > 1), \varepsilon_1(k) < 0 \quad (44c)$$

Based on (44), the proposed MPP tracking method of a second embodiment of the invention is shown as a block diagram in Fig. 14. f_s is modulated with a small-signal sinusoidal variation. V_i and \hat{v}_i are sensed. V_i is then scaled down by the factor of β and is compared with \hat{v}_i . \hat{v}_i is obtained by using a peak detector to extract the value of the ac

component in v_i . The switching frequency component in v_i is removed by using a low-pass (LP) filter. The error amplifier controls the PWM modulator to locate d at D_{MP} . If \hat{v}_i is smaller than $(\hat{f}_s / 2\bar{f}_s)V_i$, $\varepsilon_1 > 0$. The output of the error amplifier, and hence d , will be increased. Conversely, d will be decreased until $d = D_{MP}$. It can be seen from the above that the proposed technique will keep track the output characteristics of solar panels without approximating the voltage-current relationships.

B. Discontinuous Capacitor Voltage Mode (DCVM)

In this mode, r_i equals

$$r_i = \frac{(1-d)^2}{2f_s C} \quad (45)$$

Thus, δr_i with respect to the frequency variation δf_s is

$$\delta r_i = -\frac{(1-d)^2}{2\bar{f}_s^2 C} \delta f_s. \quad (46)$$

Similar to deriving (38) and (40), it can be shown that

$$V_i = \frac{(1-d)^2}{(1-d)^2 + (1-D_{MP})^2} v_g \quad (47)$$

$$\text{and } \hat{v}_i = \frac{(1-d)^2 (1-D_{MP})^2 v_g}{[(1-d)^2 + (1-D_{MP})^2]^2 \bar{f}_s} \hat{f}_s \quad (48)$$

By substituting $d = D_{MP}$ into (37) and (48), (42) is still valid. Again, the

difference, ε_2 , between the nominal characteristics of $\frac{\hat{f}_s V_i}{2\bar{f}_s v_g}$ and $\frac{\hat{v}_i}{v_g}$ can be shown to be

$$\varepsilon_2(k') = \frac{\hat{f}_s V_i}{2\bar{f}_s v_g} - \frac{\hat{v}_i}{v_g} = \frac{\beta k'^2 (k'^2 - 1)}{(k'^2 + 1)^2} \quad (49)$$

where $k' = (1 - d) / (1 - D_{MP})$.

Fig. 15 shows the relationships between ε_2 / β and k' . Similar behaviors as in (44) are obtained

$$\text{If } d < D_{MP} (k' > 1), \varepsilon_2(k') > 0 \quad (50a)$$

$$\text{If } d = D_{MP} (k' = 1), \varepsilon_2(1) = 0 \quad (50b)$$

$$\text{If } d > D_{MP} (k' < 1), \varepsilon_2(k') < 0 \quad (50c)$$

Hence, the control method used when the converter is operated in DICM can also be applied to a converter operated in DCVM.

C. Comparison of DICM and DCVM

Although a converter operating in DICM and DCVM can perform the MPP tracking in accordance with this embodiment of the invention, selection of a suitable operating mode is based on several extrinsic and intrinsic characteristics. Table I shows a comparison of the converter behaviors in DICM and DCVM.

Table I Comparisons of the converter behaviors in DICM and DCVM

	DICM	DCVM
M	$\frac{d}{d_1}$	$\frac{d_1}{1-d}$
r_i	$\frac{2L_e f_s}{d^2}$	$\frac{(1-d)^2}{2f_s C}$
ΔI_1	$\frac{2L_2}{d(L_1 + L_2)} I_1$	Negligible as $L_1 \gg \frac{1}{(2\pi f_s)^2 C}$

$V_{s, \max}$ and $V_{D, \max}$	$(1 + M)V_i$	$\frac{2M}{d_1}V_i$
$I_{s, \max}$ and $I_{D, \max}$	$\frac{2}{M d_1}I_1$	$(1 + \frac{1}{M})I_1$
d_1	$\sqrt{2 L_e f_s / R}$	$\sqrt{2 R f_s C}$
Condition of d	$< 1 - d_1$	$> d_1$
Application	High voltage, low current	Low voltage, high current
Recommended arrangement for solar panels	Series connection	Parallel connection

For the extrinsic characteristics, apart from the difference in the voltage

conversion ratio M , the input current ripple ΔI_1 in the DCVM is smaller than that in the DICM. Thus, variation of the panel-converter operating point in the DCVM is smaller.

This can effectively operate the panel at the near MPP. Nevertheless, input current perturbation is designed to be less than 10% in the implementation.

In order to ensure that the converter is operating in the DICM,

$$d < 1 - \sqrt{\frac{2 L_e f_s}{R}} = \frac{V_o}{V_o + V_i} \quad (51)$$

Thus, (51) gives the maximum duty cycle of S for a given load resistance.

In order to ensure that the converter is operating in DCVM,

$$d > \sqrt{2 R f_s C} = \frac{V_o}{V_o + V_i} \quad (52)$$

(52) gives the minimum duty cycle of S for a given load resistance.

For the intrinsic characteristics, the voltage stress $V_{S,\max}$ of S in the DCVM is higher than that in the DICM under the same panel terminal voltage and voltage conversion ratio. Conversely, the current stress $I_{S,\max}$ in the DICM is higher than that in the DCVM with the same panel output current. Thus, for the same panel power, DICM is more suitable for panel in series connection whilst DCVM is for parallel connection.

This second embodiment of the invention may be verified by means of the experiment setup shown in Fig.16. A solar panel Siemens SM-10 with a rated output power of 10W is used. Two SEPICs, which are operating in DICM and DCVM, respectively, have been prototyped. The component values of the two converters are tabulated in Table II.

Table II Component values of the two converters

	DICM	DCVM
L_1	2.2mH	2.2mH
L_2	25 μ H	450 μ H
C	100 μ F	47nF
C_o	1mF	1mF
R	10 Ω	10 Ω
\bar{f}_s	50kHz	50kHz
\hat{f}_s	10kHz	10kHz
f_m	1kHz	1kHz

The switching frequency is 50kHz. The modulating frequency f_m is 1kHz. The maximum frequency deviation \hat{f}_s is 10kHz. Based on Table I and (31), the maximum value of d is 0.5 for the converter in DICM. The minimum panel output resistance that can be matched by the converter is 9.8Ω . For the converter in DCVM, based on Table I and (35), the minimum value of d is 0.217. The maximum panel output resistance that can be matched is 130.5Ω . The surface temperature of the panel is kept at about 40°C throughout the test. The radiation illuminated is adjusted by controlling the power of a 900W tungsten halogen lamp using a programmable dc supply source – Kikusui PCR 2000L. Fig. 17 shows the $P_o - r_i$ characteristics of the solar panel at different P_{lamp} . It can be seen that the output resistance of the panel at MPP varies from 18Ω to 58Ω when P_{lamp} is changed from 900W to 400W. The operating range is within the tracking capacity (i.e., the input resistance) of the two converters. Fig. 18 shows the experimental waveforms of v_i and i_i of the two prototypes at the MPP when P_{lamp} equals 900W. It can be seen that v_i has a small sinusoidal perturbation of 1kHz. Fig. 19 shows the experimental voltage and current stresses on S and D in the two converters. As expected, the current stresses on S and D in the DICM are about three times higher than that in the DCVM, whilst the voltage stresses on S and D in the DCVM are four times higher than that in the DICM. These confirm the theoretical prediction.

An insolation change is simulated by suddenly changing P_{lamp} from 400W to 900W. The transient waveforms of v_i and i_i of the two converters are given in Fig. 20. It was found that both converters can perform the MPP tracking function and the panel output power is increased from 2.5W to 9.5W in 0.3sec in both cases. The tracked power is in close agreement with the measurements in Fig. 17.

It will thus be seen that at least in preferred forms of the invention novel techniques are provided for tracking the MPP of a solar panel in varying conditions. Both embodiments use either a PWM dc/dc converter, for example a SEPIC or Cuk converter. In a first embodiment of the invention a small perturbation is introduced into the duty cycle of the converter operating in discontinuous capacitor voltage mode. In the second embodiment of the invention a PWM dc/dc converter operating in discontinuous inductor-current or capacitor-voltage mode is used to match with the output resistance of the panel. In this second embodiment of the invention a small sinusoidal variation is injected into the switching frequency and comparing the maximum variation and the average value at the input voltage, the MPP can be located. Both embodiments are simple and elegant without requiring any digital computation and approximation of the panel characteristics.